

静止荷重を受ける片持および両持はり (3/4)

はりの種類	反力および曲げモーメント	たわみおよび傾斜
	$R_1 = \frac{w}{2l}(2l_2 + l_3^2 - l_2^2)$ $R_2 = \frac{w}{2l}(2l_3 + l_2^2 - l_3^2)$ $l_1 + l_2 \leq x_3 \leq l \text{ において}$ $M_{x_3} = \frac{w}{2l}[-ll_1(l_1 + 2l_2) + \{2l(l_1 + l_2) + (l_3^2 - l_2^2)\} - lx_3^2]$ $l_2 < l_3 \text{ の場合}$ $x_3 = (l_1 + l_2) + \frac{l_3^2 - l_2^2}{2l} \text{ において}$ $M_{\max} = \frac{w}{8l^2}[4ll_3(l_3(l_1 + l_2) + l_2^2) + (l_3^2 - l_2^2)^2]$	$\delta_{x_3} = \frac{wl}{24EI} [l\{(l_1 + l_2)^4 - l_2^4\} + \{2l^2(l_3^2 + 2l_2^2) - 4l(l_1 + l_2)^3 - (l_3^4 - l_2^4)\}x_3 + 6l\{(l_1 + l_2)^2 - l_2^2\}x_3^2 - 2\{2l(l_1 + l_2) + (l_3^2 - l_2^2)\}x_3^3 + lx_3^4]$
	$R_1 = \frac{\bar{W}}{3} \quad R_2 = \frac{2\bar{W}}{3}$ $M_x = -\frac{\bar{W}x}{3}\left(1 - \frac{x^2}{l^2}\right)$ $M_{\max} = -\frac{2}{9\sqrt{3}}\bar{W}l = 0.128\bar{W}l$ $[x = 0.5774l \text{ において}]$	$\delta_x = \frac{\bar{W}l^3}{180EI} \left(\frac{7x}{l} - \frac{10x^3}{l^3} + \frac{3x^5}{l^5} \right)$ $\delta_{\max} = 0.01304 \frac{\bar{W}l^3}{EI}$ $[x = l\sqrt{1 - \sqrt{8/15}} = 0.5193l \text{ において}]$
	$R_1 = R_2 = \frac{\bar{W}}{2}$ $M_x = \bar{W}x \left(\frac{1}{2} - \frac{x}{l} + \frac{2x^2}{3l^2} \right)$ $M_{\max} = \frac{\bar{W}l}{12}$	$\delta_x = \frac{\bar{W}l^3}{12EI} \left(\frac{3x}{8l} - \frac{x^3}{l^3} + \frac{x^4}{l^4} - \frac{2x^5}{5l^5} \right)$ $\delta_{\max} = \frac{3\bar{W}l^3}{320EI} = \frac{9f_b l^2}{40Eh}$
	$R_1 = R_2 = \frac{\bar{W}}{2}$ $M_x = \bar{W}x \left(\frac{1}{2} - \frac{2x^2}{3l^2} \right)$ $M_{\max} = \frac{\bar{W}l}{6}$	$\delta_x = \frac{\bar{W}l^3}{12EI} \left(\frac{5x}{8l} - \frac{x^3}{l^3} + \frac{2x^5}{5l^5} \right)$ $\delta_{\max} = \frac{\bar{W}l^3}{60EI} = \frac{f_b l^2}{5Eh}$
	$R_1 = R_2 = \frac{W}{2}$ $M_x = \frac{Wl}{2} \left(\frac{x}{l} - \frac{1}{4} \right)$ $M_{x_1} = \frac{Wl}{2} \left(\frac{x_1}{l} - \frac{3}{4} \right)$ $M_{\max} = \frac{Wl}{8}$	$\delta_x = \frac{Wl^3}{16EI} \left(\frac{x^2}{l^2} - \frac{4x^3}{3l^3} \right)$ $\delta_{\max} = \frac{Wl^3}{192EI} = \frac{f_b l^2}{12Eh}$ $i_x = \frac{Wl^2}{8EI} \left(\frac{x}{l} - \frac{2x^2}{l^2} \right)$ <p style="text-align: right;">(中央にて)</p>
	$R_1 = \frac{Wl_2^2(3l_1 + l_2)}{l^3}$ $R_2 = \frac{Wl_1^2(l_1 + 3l_2)}{l^3}$ $M_A = -\frac{Wl_1l_2^2}{l^2}, \quad M_B = -\frac{Wl_1^2l_2}{l^2}$ $M_c = -\frac{Wl_1l_2^2}{l^2} + \frac{Wl_2^2x(3l_1 + l_2)}{l^3}$ $M_{x_1} = \frac{Wl_1^2(l_1 + 2l_2)}{l^2}$ $\frac{Wl_1^2x_1(l_1 + 3l_2)}{l^3}, \quad M_O = \frac{2Wl_1^2l_2^2}{l^3}$	$\delta_x = \frac{Wl_2^2x^2}{6EI} \left\{ \frac{3l_1}{l} - \frac{(3l_1 + l_2)x}{l^2} \right\}$ $\delta_{x_1} = \frac{Wl_2^2x_1^2}{6EI} \left\{ \frac{3l_1}{l} - \frac{(3l_1 + l_2)x_1}{l^2} \right\} + \frac{W(x_1 - l_1)^3}{6EI}$ $\delta_c = \frac{Wl_1^3l_2^3}{3EI l^3}$ $l_1 > l_2 \text{ のとき } x = \frac{2l_1l}{3l_1 + l_2} \text{ において}$ $\delta_{\max} = \frac{2Wl_1^3l_2^3}{3EI(3l_1 + l_2)^3}$ $l_1 < l_2 \text{ のとき } x = \frac{l_1 + 3l_2}{l} \text{ において}$ $\delta_{\max} = \frac{2Wl_1^2l_2^3}{3EI(l_1 + 3l_2)}$

応力 $\sigma = \frac{M}{Z}$

$I = \frac{\pi}{64} d^4$

$Z = \frac{1}{16} d^3$

M: 曲げモーメント

I: 断面二次モーメント

Z: 断面係数

d: 材料直径

E: 係数弾性係数